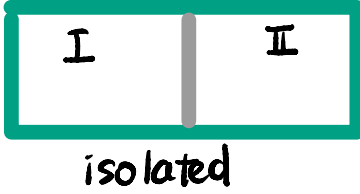


## 2-2 walls / constraints.



- rigid wall: mechanical work
- adiabatic wall: ~~X~~ heat
- diathermal wall: ~~✓~~ heat

## 2-3 First Law of thermo.

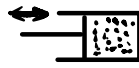
$$\uparrow \Delta U$$

$$1 \rightarrow \underline{dU} = \underbrace{\delta Q + \delta W}_{\text{Transitory}}$$

$U \rightarrow$  a definite state

$W_M$   
 $W_E$   
 $W_C$

$$\delta W = -pdV$$



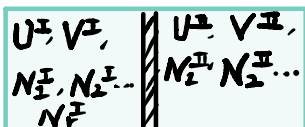
$\left\{ \begin{array}{l} dW > 0 \text{ sys gains energy.} \\ dW < 0 \text{ sys loses energy} \end{array} \right.$

$$\delta Q = dU - \delta W = dU + PdV$$

$$\Rightarrow dU_{\text{total}} = 0 = dU_{\text{sys}} + dU_{\text{surr.}}$$

$$\Rightarrow dU_{\text{sys}} = -dU_{\text{surr.}}$$

## 3. Basic Problem (Abstract)



isolated

\*. Determine equilibrium state after removal of certain constraints in an isolated sys.

#### 4. Postulates & Fundamental Equations.

\* here formulate the solutions by a series of postulates.

t-dependent evolution in Q.M.

$$\frac{\partial}{\partial t} |\psi(t)\rangle = -\frac{i}{\hbar} \hat{H} |\psi(t)\rangle$$

For thermo.

$$\frac{d}{dt} S(t) \geq 0$$

↓ Entropy

Postulate I: There exists a function

$S = S(U, V, N_1, N_2, \dots)$  of extensive parameters defined for equilibrium states,  $U, V, N_1, \dots$  tend to maximize  $S$ .

Fundamental relation.

Postulate II.

$S$  of a composite system.

\* additive  $S = \sum_i S^{(i)}$

\*. continuous & differentiable w/ respect to U

\*.  $U \uparrow \Rightarrow S \uparrow$

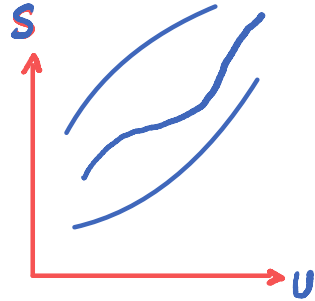
→ S is 1<sup>st</sup>-order function of extensive parameters

$$S = S(U, V, N_1, \dots)$$

$$\lambda = \text{const.}$$

$$S' = S(\lambda U, \lambda V, \lambda N_1, \dots)$$

$$= \lambda S(U, V, N_1, \dots)$$



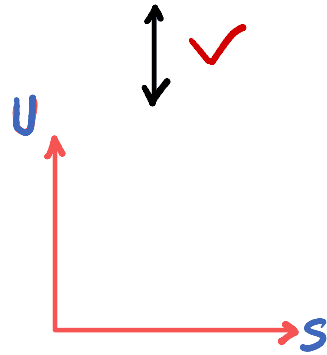
→  $S(U, V, N)$  can be inverted w/ respect U.

↓

\*  $U = U(S, V, N)$

$$\left( \frac{\partial S}{\partial U} \right)_{V, N_1, N_2, \dots} > 0$$

$$\Downarrow \\ 1/T$$



## Postulate II

"S" vanish is  $\left( \frac{\partial U}{\partial S} \right)_{V, N_1, \dots} = 0$ .

(3<sup>rd</sup> law of thermo, or "Nernst Postulate")

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Obj. #2. Equilibrium process / conditions.

1. Intensive Parameters. ( $T \rightarrow U(S, V, N)$ ).
  2. Equation of states ( $PV = NRT$ )
  3. The entropic intensive parameters.
  4. Different types of equilibrium.
    - Thermal
    - Mechanical.
    - Matter flow
    - chemical
- 

1. Intensive Parameters.

\* P.D.

def continuous function of multivariables.

$$\Psi = \Psi(x, y, z)$$

if  $y, z = \text{const}$ .  $\Psi = \Psi(x)_{y, z}$

the derivative is so-called P.D. w/ respect to

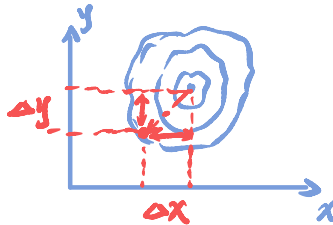
$x$ , and denoted as  $(\frac{\partial \psi}{\partial x})_{y,z}$

\*. For 1<sup>st</sup>-order differential.  $\psi(x, y, z)$

$$d\psi_x = \left( \frac{d\psi(x, y_0, z_0)}{dx} \right) \cdot dx = \left( \frac{\partial \psi}{\partial x} \right)_{y,z} dx$$

$$d\psi_y = \left( \frac{\partial \psi}{\partial y} \right)_{x,z} \cdot dy \quad d\psi_z = \left( \frac{\partial \psi}{\partial z} \right)_{x,y} dz$$

$$d\psi = d\psi_x + d\psi_y + d\psi_z$$



\*.  $U = U(S, V, N_1, \dots, N_r)$

$$dU = \left( \frac{\partial U}{\partial S} \right)_{V, N_1, \dots} dS + \left( \frac{\partial U}{\partial V} \right)_{S, N_1, \dots} dV + \left( \frac{\partial U}{\partial N_2} \right)_{S, V, N_3, \dots} dN_2$$

$\downarrow$   
 $T$

$\downarrow$   
 $-P$

$\downarrow$   
 $\mu$

$$dU = \underline{dQ} + \underline{dW}$$

$$\Rightarrow dQ = T \cdot dS$$

$$dW \begin{cases} dW_M = -P dV \\ dW_C = \sum_i \mu_i dN_i \end{cases}$$